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**Effects of Biomass Growth on Pressure Drop in Submerged Aerated  
Bioreactors**

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**1-Introduction**

Submerged aerated biological filter SBAF is economically efficient technology for industrial wastewater, and also used for the biological treatment of moist, dilute airstreams contaminated with odorous, toxic, and volatile organic compounds (Leson and Winer 1991; Swanson and Loehr 1997; Wani et al. 1997). The pollutants are degraded by a microbial community that develops under optimized conditions of humidity, temperature, and pH within the bed.

In a biofilter, the synthesis of microbial mass (biomass) by the mineralization of biodegradable pollutants leads to biomass growth and accumulation over time, which has been related to an increase in flow resistance in the bed [e.g., Kinney et al. (1996) and Mohseni et al. (1998)]. Biomass accumulation, which is greater at the inlet sections of biofilters (Corsi and Seed 1995; Swanson and Loehr 1997), leads to a change in bed characteristics, such as the reduction of the interparticle void space and the compaction of natural packing materials, which cause channeling and increased pressure drops. This translates into higher operating and maintenance costs that become significant for long-term biofilter operation. A better understanding of the growth of biomass in biofilters and the effects on flow may lead to improved designs with reduced energy requirements, lower operating and maintenance costs, and increased removal capacities. This knowledge will also help to identify sources of operational problems and to formulate measures for improving the biofiltration process.

Three distinct approaches to model microbial growth and accumulation processes in porous media include the continuous biofilm, discrete micro colony, and macroscopic approaches (Baveye and Valocchi, 1989). The biofilm approach assumes continuous and uniform biomass growth on the exposed surface of each particle in a porous medium. Taylor and Jaffe (1990a, b, c) and Taylor et al. (1990) used this assumption to derive analytical expressions to model changes in porous media properties due to biological growth. However, as pointed out by Baveye and Valocchi(1989), Taylor and Jaffe's (1990) experimental study presented no supporting evidence to verify the actual growth patterns and film thicknesses of the attached biomass. Cunningham et ai. (1991) also proposed expressions to model the influence of biofilm accumulation on hydrodynamics in porous media. However, use of these expressions is limited to cubically packed spherical media with particles of uniform diameter Alternatively, Vandevivere and

Baveye (1992a, b) support the microcolony model for biomass growth since they observed discrete microbial colonies in a biologically active saturated sand column. Microbial growth inside the column was sparse and heterogeneous. In reality, growth patterns in porous media are more likely a combination of the two models, where microbes initially grow in discrete colonies and gradually expand to form continuous biofilms (Rittmann, 1993). Therefore, the macroscopic approach, the third alternative which considers only spatially averaged biomass concentrations, is a more realistic option for describing biomass in porous media. This option offers more adaptability because it does not suppose any specific growth pattern. It is also the approach most commonly reported in the literature (Corapcioglu and Haridas, 1984; Borden and Bedient, 1986; and Kindred and Celia, 1989). Moreover, in most microbially mediated transport studies involving porous media, experimental data for microbes are reported only as average biomass concentrations (Taylor and Jaffe, 1990; Lundman, 1992; Lozada et al., 1994; and Jennings, 1994). The biomass layers appeared very gel-like and had a high water content and high concentration of extracellular polymeric substances (EPSs) (Farrugia 1999; Morgan-Sagastume 1999).

The pressure drop through a biofilter bed typically ranges from 20 to 100 Pa/m and can even go up to 1000 Pa/m, and typical superficial air velocities may vary from 5 to 500 m<sup>3</sup>/m<sup>2</sup> h (Devinny et al. 1999). Systems with adequate moisture control and a porous medium containing bulking agents will typically achieve pressure losses <900–1,700 Pa/m (Leson and Smith 1997).

Various researches have reported flow pressure losses in biofilters in relation to the bed particle size (Van Langenhove et al. 1986; Allen and Yang 1991; Corsi and Seed 1995); nature and composition of the filter medium (Shareef-deen et al. 1993; Mohseni et al. 1998); bed content (Sabo et al. 1993); and time of operation. Some studies have related increases in pressure drop to biofilm growth and clogging by biomass (Utkin et al. 1989; Hodge et al. 1992). For example, Liu et al. (1994), working with granular activated carbon columns for toluene removal, measured increased pressure drops of up to 12 kPa/m due to biomass accumulation and airflow channeling. In general, the increase in pressure drop as a result of biomass development in biofilters can be explained by a decrease in the bed interparticle void space or the effective porosity or both and by the microbial degradation of the support matrix, as in the case of natural media, which result in decreased specific permeability. Although the effect of biomass accumulation on pressure drop has been studied in biotrickling filters treating a gaseous stream (Soriat et al. 1997; Okkerse et al. 1999), there has not been detailed, quantitative research on this phenomenon in biofilters.

***The aim of this paper*** is to:-

- Model changes in porosity and specific surface area caused by biomass accumulation in porous media. the macroscopic approach is adopted and used attached biomass concentration as the model variable to describe variations in porous media properties.
- Study the influence of biomass accumulation on pressure drop in submerged biological aerated reactor that treat organic compounds.
- Model pressure losses caused by biomass growth in SABR using semi empirical models.
- Evaluate the interparticle porosity and pressure drop changes due to biomass accumulation in a SABR.

## **2-Experimental Approach**

### **2-1-Experimental Setup**

A biofiltration system consisting of two identical laboratory scale SABRs were used to treat industrial wastewater Plate(1). For each biofilter, wastewater was passed through stainless steel column (100mm diameter and 1m height), packed and regulate its temperature in the SABR in the range of 24 – 26°C.



A small and controlled airflow from the inlet air-stream was compressed and passed through a stainless-steel vessel which then was fed to the top of the SABR. The biological oxygen demand BOD<sub>5</sub>, chemical oxygen demand COD, and total solids TS were monitored every run from wastewater samples taken at the inlet and the outlet of each SABR. Manometer was used to measure differential pressure along segments of the beds, between axial ports located at the top, middle, and bottom of each section. The minimum detectable differential pressure reading of the manometer was 2.5 Pa (0.25mm. water). The amount of biomass developed on the packing materials was assessed in both biofilters from bed composite samples taken from the top and bottom of each bioreactor.

Sampling was performed on a periodic basis, every 2–3 weeks. In total, eight samplings were performed during this experiment. After sampling, the packing material within each biofilter was remixed to ensure a uniform biomass distribution at the beginning of each period of operation.

### **2-2-Packing Media**

One SABR was packed with sieved porcelinite rock (1228kg dry /m<sup>3</sup> bioreactor) with a size range of (2.5-4mm). These types of porcelinite rock were used successfully in previous biofiltration experiments. The other SABR was packed with polystyrene (32 kg dry /m<sup>3</sup> bioreactor; with diameters of (4-6mm), Eight liters of packing material were randomly packed in each SABR s.

The polystyrene have been successfully used in SABRs, and they were used in this experiment because they provide interference-free biomass quantification and have a defined spherical shape and size for pressure drop modeling.

### **3-Hydrodynamic Modeling**

In packed beds with biofilm growth, if the biofilm thickness remains small compared to the effective pore space, accumulation of biofilm will not significantly affect the distribution of fluid velocities within a porous medium (Cunningham et al . 1990). However, if the biofilm occupies a significant fraction of the effective pore space, a decrease in porosity will occur as shown in Fig.(1). Alonso et al. (1997) developed a model to describe physical and biological processes taking place in a biotrickling filter for waste quantities into dimensional parameters it is possible to reduce the number of variables appearing and to make this compact results ((equation or chart) applicable to all similar situation.

Investigations consider the bed of porous media as composed of a number of capillary pores, passing in parallel, straight through the depth of the bed .In this case the head loss in high flow velocity (turbulent flow) depend upon capillary water velocity ( $V_c$ ), dynamic viscosity ( $\mu$ ), density ( $\rho$ ). Using dimensional analysis (Buckingham  $\Pi$  theorem), general form of the empirical relationship can be constructed as follow: -

$$\frac{\Delta H}{L} = \Psi(\text{Re}) \frac{1}{d_c} \frac{V_c^2}{2g}$$

(1)

$$V_c = \frac{Q}{nA_b} = \frac{V \cdot \zeta}{n} \text{-----}$$

(2)

$$\text{And } n = \frac{\nabla_v}{\nabla} \text{-----}$$

-- (3)

Where  $L$ : length of capillary (L),  $\mu$ : dynamic viscosity (M/L.T),  $\rho$ : density (M/L<sup>3</sup>),  $g$ : standard acceleration of gravity, (9.81m/s<sup>2</sup>),  $d_c$ : inside diameter of capillary(L) and  $V_c$ : velocity of fluid in capillary (L/T).  $n$ : bulk porosity of bed of porous media (L<sup>3</sup>/L<sup>3</sup>),  $\nabla_v$ : volume of the voids (L<sup>3</sup>),  $\nabla$ : total volume of the bed (L<sup>3</sup>),  $\zeta$ : tortuosity (L/L).

$\Psi(Re)$  is function to Reynolds number ( $Re$ ) which is one of the most important dimensionless parameters in high flow velocity in porous media and its size determines the nature of flow. Turbulent flow in pipe, friction factor can be evaluated from (Blasius formula): -

$$f = \frac{0.316}{Re^{0.25}} \text{-----}$$

(4)

Similar to (Blasius formula) the hydraulic resistance factor ( $C_f$ ) in porous media can be simulated as function to friction factor and as the form: -

$$C_f = \frac{C'_f}{Re^{.25}} \text{-----}$$

(5)

$$\text{And } Re_{pore} = \frac{4\zeta \rho V}{\mu (1-n) S} \text{-----}$$

(6)

Where  $C'_f$ : constant depends upon porosity( $n$ ), uniform factor ( $\Phi$ ), and grain shape of media. Because of extreme complexity of grains shape of the media and its arrangement (spacing between the grains) most of the advance in understanding the basic relation have been developed around experiments on grains shape or initial specific surface area per volume of clean substratum (m<sup>2</sup>/m<sup>3</sup>),  $S_o$  which is defined as:

$$S_o = \frac{3(1-n_o)}{\phi \cdot R} \text{-----}$$

----- (7)

The average shape or sphericity factor for the porcelinite spherical grain size was assumed to be 0.85, based on values of (0.75-0.95) for nearly spherical of various sand types (Perry and Green 1988). The expression proposed for calculating biomass-affected porosity  $n_b$  in a bed packed with spheres, where biomass grows uniformly on the sphere surfaces (Fig.(1)):

$$n_b = n_o - n_{iv} \text{-----}$$

(8)

$$\nabla_{mr} = \frac{1-n_b}{1-n_o} \text{-----}$$

----- (9)

$$\nabla_{mr} = \left(1 - \frac{L_b}{R}\right)^3 - \frac{N}{4} \left(\frac{L_b}{R}\right)^2 \left(2\frac{L_b}{R} + 3\right) \text{-----}$$

---- (10)

where :  $\phi$  = sphericity factor for the packing solids;  $n_0$  = initial porosity of the bed without biofilm  $L^3/L^3$ ;  $n_b$  = the biomass-affected porosity;  $n_{fv}$  = Volume fraction of the biomass ( $L^3$  biomass/  $L^3$  total);  $L_b$  = biofilm thickness ( L );  $\forall_{mr}$  = accumulative volume ratio of the packing medium ( $L^3$  biomass/  $L^3$  bed);  $R$  = radius of a sphere equivalent to the packing medium L ; and  $N$  = number of packing spheres in contact with a single sphere or coordination number. Eq. (10) was deduced for spheres in contact, upon which biofilm grow uniformly, leaving the contact points uncovered. The coordination number  $N$  that accounts for the number of contact points among the spheres can be estimated from an expression (Dullien 1992) correlating porosity  $n$  and the coordination number for a close random type of packing

$$N = 13.84 \pm \sqrt{(191.4 - 231.9 n)} \text{-----}$$

----- (11)

The thickness  $L_b$  of the biofilm growing on the packing material can be calculated as follows:

$$L_b = \frac{X}{\rho_b} \text{-----}$$

----- (12)

where  $X$  = superficial biomass concentration (g biomass/m<sup>2</sup> surface area); and  $\rho_b$  = biofilm density (g biomass/m<sup>3</sup> biomass) (M biomass/L<sup>3</sup> biomass)..

The fraction of volume occupied by the solid-phase biomass can be estimated as :-

$$\forall_{mr} = \frac{\rho_s X_m}{\rho_b} \text{-----}$$

----- (13)

where  $X_m$  is the mass (dry weight) of microbial cells per unit mass of solids (M of microbial mass /M of bed). Based on volume balances, a simple macroscopic equation

Volume fraction of the biomass  $n_{fv}$  can be expressed as :-

$$n_{fv} = \frac{1}{3} \phi . R (\forall_{mr} - 1) S_o \text{-----}$$

(14)

Volume fraction of the biomass  $n_{fv}$  can be approximate as function to specific surface area, and biofilm thickness ( Taylor et al. (1990))

$$n_{fv} = L_b S_o \text{-----}$$

(15)

Using this porosity relationship, equations ( 7) and (8) are modified to estimate biomass-affected specific surface area ( $S_b$ ) values

$$S_b = \frac{3(1 - n_b)}{\phi . R (1 + \frac{L_b}{R})} \text{-----}$$

(16)

for computing specific surface area reduction , biomass-affected specific surface area ratio related to porosity ratio can be expressed as

$$\frac{S_o}{S_b} = \left(\frac{n_b}{n_o}\right)^{0.5} \text{-----}$$

-----(17)

Values of specific surface area are typically unimportant except in the biofilm approach where they are required to compute film thicknesses. Although the macroscopic approach does not explicitly consider

biofilms, it is possible to estimate apparent biofilm thicknesses through macroscopic model-based equations (17). These film thicknesses can be useful in modeling diffusion limitations across attached biomass (Rittmann and McCarty, 1981). Analytical models for predicting changes in porosity and specific surface area due to microbial growth in porous media are developed from a macroscopic approach. Variations in SABR properties are computed from macroscopic averaged attached biomass concentrations. The macroscopic models developed in this work are easy to implement and computationally more efficient than the biofilm models. The macroscopic expressions can be explicitly used to estimate biomass-affected porosity and specific surface area, at any attached biomass concentration. Since the biofilm models of Taylor et al. (1990) are implicit functions of attached biomass thickness, these porous media properties cannot be estimated explicitly.

A comparison of experimental results and estimated results based on our macroscopic biofilm models is presented for predictions of relative changes in porosity (Fig.(1)). Simulation experiments started with clean media (without biomass) which the head loss in SABR can be formulated as follow :-

$$\frac{\Delta H}{L} = C'_f \left(\frac{\mu}{\rho}\right)^{0.25} \left\{\frac{(1-n)^{1.25}}{n^3}\right\} S^{1.25} \zeta^{1.75} V^{1.75} \text{-----}$$

- (18)

Analyses of experimental results show that the effect of biomass on head loss per bed depth in SABR s can be evaluated by the modified equation

$$\frac{\Delta H}{L} = C'_f \left(\frac{\mu}{\rho}\right)^{0.25} \left\{\frac{(1-n)^{1.25}}{n^3}\right\} S^{1.25} \zeta^{1.75} V^{1.75} \nabla_{mr} \text{-----}$$

(19)

For modeling the effect of biomass on pressure drop in SABR s using the above equations, the following assumptions are made:

- the packing material is composed of homogenous particles.
- biomass grows uniformly on the surface of spheres or of other particles with an equivalent diameter of a sphere of the same surface area.
- the spheres remain in contact during biomass accumulation, which assumes biofilm growth on the whole surface of the spheres; and
- biomass has a constant density within the biofilm, which can be assumed at a macro scale, even if at a micro scale there is strong evidence of high biofilm heterogeneity (Bishop 1997).

#### **4-Experimental Results**

At the highest flow rates, the increase in pressure drop and the increase of the degree of curvature of the lines suggest that kinetic energy losses became important. The kinetic energy losses as a function of the flow rate squared and the reduction of the bed porosity Fig.(1).The general approach in modeling the effects of biomass accumulation on pressure drop in the polystyren biofilter involved estimating porosity changes and pressure drops in the SABR based on the experimental concentrations of biomass (g biolayer/g dry substratum) and on waste water flow rates (Fig.(2)).The comparsoin between the experimental results of head loss of water per bed depth and proposed equation (19) gives acceptable approximation (Fig.(3)).

Fig.(1): The effect of biofilm thickness on bed porosity for different bed materials.

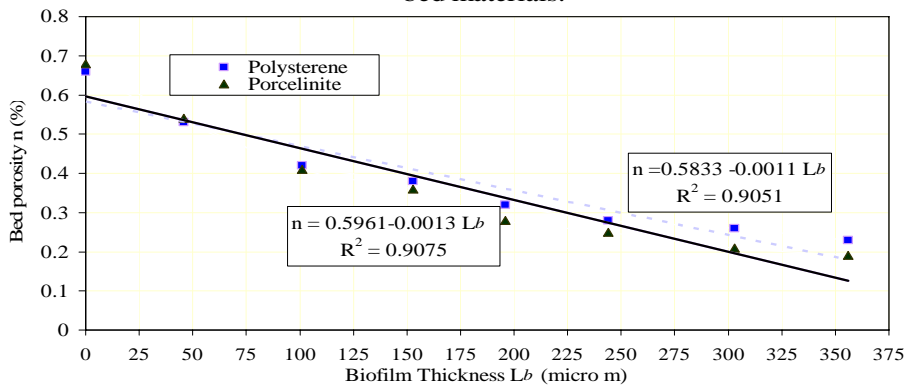
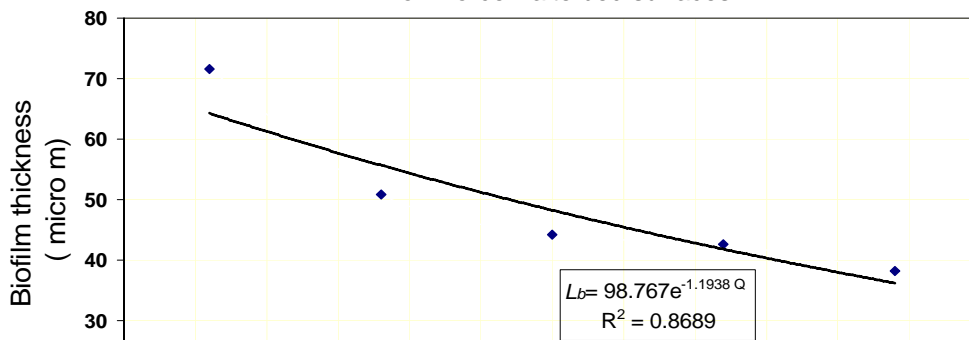


Fig.(2): The effect of influent rate in generated biofilm thickness on Porcelinaite bed surfaces.



Localized high biomass content in the SABR beds was the key factor affecting increased pressure drop in both SABRs caused by local clogging or local void space reduction or both. The effect of accumulated an incremental amount of biomass for different times and on pressure drop were correlated with a reasonable approximation in Figs.(4) to (6) . The pressure drop in the porcelinite rock biofilter was twice that in the polysteren SABR. This difference was believed to be due to greater biomass growth in the porcelinite rock bed (polysteren polysteren: 0.4–3.2 g biolayer/g dry substratum; porcelinite rock: 0.5– 19 g

biolayer/g dry substratum) and a different pore structure

Fig.(3):-The comparsoin between proposed and measured head loss per bed depth in Porcelinaite SABR

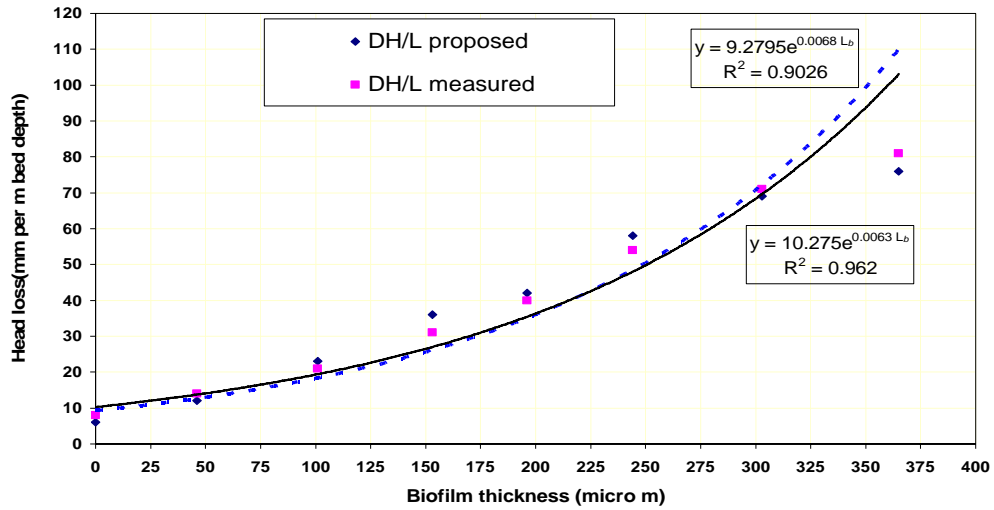
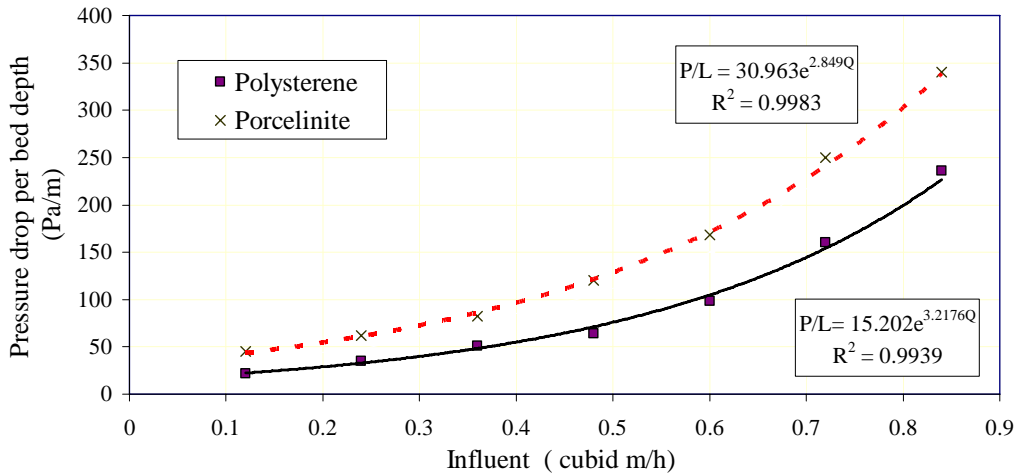
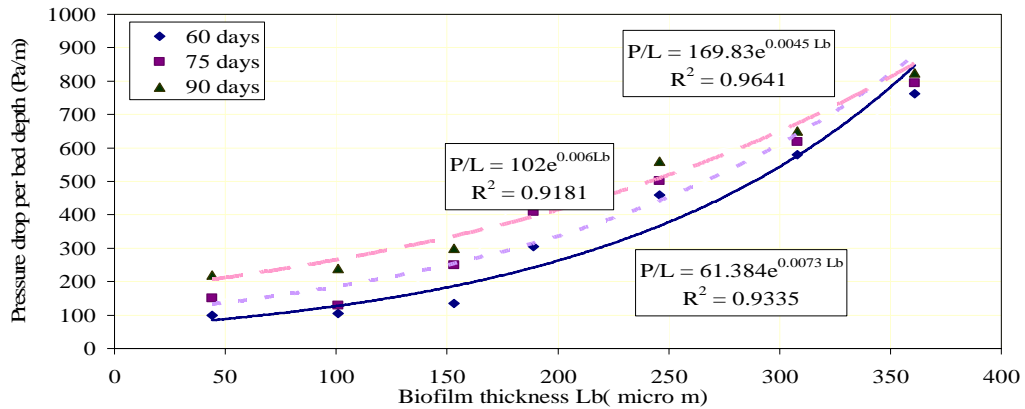


Fig.(4): The effect of influent on pressure drop per unit bed depth of SABR for different clean bed materials.



Biofilm thickness values were first estimated from the biomass concentrations (g biolayer/g dry substratum) in the bed. For this, the biomass concentrations were converted from grams of biolayer per grams of dry substratum to grams of biomass per square meters of substratum surface, using the dry substratum bulk density and an estimated initial superficial area of the packed substratum .

Fig.(5): The effect of biofilm thickness on pressure drop per Porcelainite bed depth in SABR .



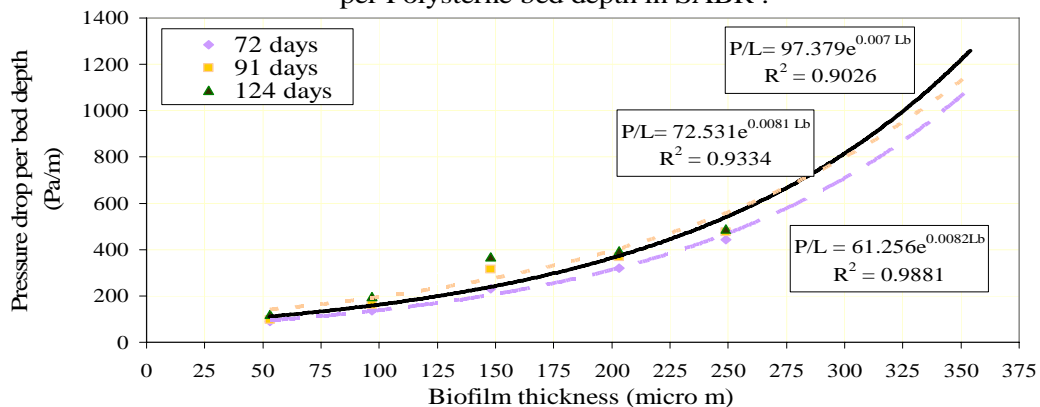
Differences between predicted and experimental pressure drops in the polystyrene SABR and porcelainite rock SABR before remixing are due to uneven biomass distribution at high biomass concentrations, which is not thoroughly characterized by averaging biomass concentration over a specific bed volume.

The profiles of detached biolayer for both the polystyrene SABR and porcelainite rock SABR show that most of the biomass accumulated in the first half of the bed and the biomass concentrations in the porcelainite rock bed were roughly 180% to 210% higher than in the polystyrene SABR. The biomass accumulation on the porcelainite rocks bed played the main role in controlling the pressure drop increase, compared to compaction.

High concentrations at the top of both the polystyrene SABR and porcelainite rock SABR on day 76 in the porcelainite rock SABR correspond to the observed formation of biomass layers (0.3–0.4 cm) on the top of these sections, which caused the highest pressure drops during the experimental period

Biomass water content in these layers was as high as 29–61 g water/g TS in the polystyrene biofilter, compared to 13–15g water/g TS in the rest of the bed, and in the porcelainite biofilter as high as 97–122g

Fig.(6): The effect of biofilm thickness on pressure drop per Polysterne bed depth in SABR .



### 5-Summary and Conclusions

5-1 Asemi empirical model was developed to predict pressure drop from biomass concentrations in a SABR bed by modification the pressure drop in porous media equation as a function of bed porosity and biomass affected porosity. -The model is a good estimate for predicting biomass-affected porosity in beds packed with spherical particles where biomass grows evenly distributed, and it successfully predicts pressure drop for the case of even biomass growth on spherical particles as follow: -

$$\frac{\Delta H}{L} = C'_f \left(\frac{\mu}{\rho}\right)^{0.25} \left\{\frac{(1-n)^{1.25}}{n^3}\right\} S^{1.25} \zeta^{1.75} V^{1.75} \nabla_{mr}$$

5-2 The optimal utilization of a SABR bed strongly depends on biomass distribution within the bioreactor and not just on the amount of biomass growing on the packing material. The highest pressure drops in the beds were caused by layers of biomass which increased the biomass specific volume and significantly decreased the bed porosity at the top levels of the biofilters.

5-3 porcelinite rocks SABR caused greater pressure drops, on average 2 times higher than the polystyrene SABR. Compaction, as a consequence of biomass growth degradation, together with water content, increased the pressure drop in the porcelinite rocks bed.

5-4 The proposed models can be used as simple tools for estimating changes SABR properties during biological process.

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